



acm International Collegiate
Programming Contest



UC Programming Contest 2006 Contest Session Universidad de Carabobo, Venezuela

September 29, 2006

This problem set should contain a rules section and seven (7) problems on fifteen (15) numbered pages. Please inform the Contest Staff immediately if something is missing from your problem set.
Welcome to the Programming Contest and enjoy it!

Rules

- Each team will be provided with a single computer. All teams will have equivalent computing equipment.
- There are seven (7) problems for each team to be completed in four (4) hours.
- All problems require that you read test data from the *standard input* and write results to the *standard output*.
- You may use any of the following programming languages: C, C++ or Java. You may use different programming languages for different problems and even for different submissions of a problem.
- All problems have a source file name shown below the title of the problem. The extensions you must use for your source files are: *.c* for programs written in C, *.cpp* for those in C++, and *.java* for those in Java.
- You may use any of the standard libraries that your chosen programming language provides. You may not use any other library that requires an extra flag to be passed to the compiler command. If you do this, judges will probably get a compilation-linking error in your program.
- Output corresponds exactly to the provided sample output format, including (mis)spelling and spacing. Multiple spaces will not be used in any of the judges' output, except where explicitly stated.
- Your solution to any problem should be submitted for judging using PC² software only. Once you have submitted a solution, it will reach the judges. The time it takes for your problem to be judged will depend on how busy the judges are. Once your submission has been judged, you will receive a message through PC² indicating the judgment. If your solution is accepted the message will be "Yes", if it's not then the message will be "No", along with the type of error the judges encountered, which may be: "Compilation Error", "Run-time Error", "Time-limit Exceeded", "Wrong Answer", "Excessive Output", "Incomplete Output" or "Output Format Error".
- Programming style is not considered in this contest. The judges will only test whether the input / output behavior of your program is correct or not. However, each problem has an execution time-limit of 90 seconds. That is, if your program takes more than 90 seconds to execute for the given input, it will be judged as incorrect.
- Contestants may bring any printed materials (books, papers, documentation, source code of programs, etc.) to the contest area, but no soft copy will be allowed (diskettes, CDs, DVDs, pen-drives, etc.).

1 S-Trees

Source file name: `streets.c`, `streets.cpp` or `streets.java`

A Strange Tree (S-tree) over the variable set $X_n = \{x_1, \dots, x_n\}$ is a **complete** binary tree representing a Boolean function $f : \{0, 1\}^n \rightarrow \{0, 1\}$. Each of the S-tree's nodes has a depth, defined as the number of nodes in the path from the root to itself minus 1 (so the root has depth 0). The depth of any node in an S-tree is at most n . The nodes with depth less than n are called *non-terminal nodes*, each having two children: the right child and the left child. Each non-terminal node is labeled with some variable x_i from the variable set X_n . All non-terminal nodes with the same depth are labeled with the same variable, and non-terminal nodes with different depth are labeled with different variables. So, there is a unique variable x_{i_0} corresponding to the root, a unique variable x_{i_1} corresponding to the nodes with depth 1, and so on. The sequence of the variables $x_{i_0}, x_{i_1}, \dots, x_{i_{n-1}}$ is called the variable ordering. The nodes having depth n are called *terminal nodes*. They have no children and are labeled with either 0 or 1. Note that the variable ordering and the distribution of 0's and 1's on terminal nodes are sufficient to completely describe an S-tree.

As stated earlier, each S-tree represents a Boolean function f . If you have an S-tree and values for the variables x_1, \dots, x_n , then it is quite simple to evaluate $f(x_1, \dots, x_n)$: Start at the root and repeat the following steps: if the node you are at is labeled with a variable x_i , then depending on whether the value of x_i is 1 or 0, you go to its right or left child, respectively. Once you reach a terminal node, its label gives the value of the function.

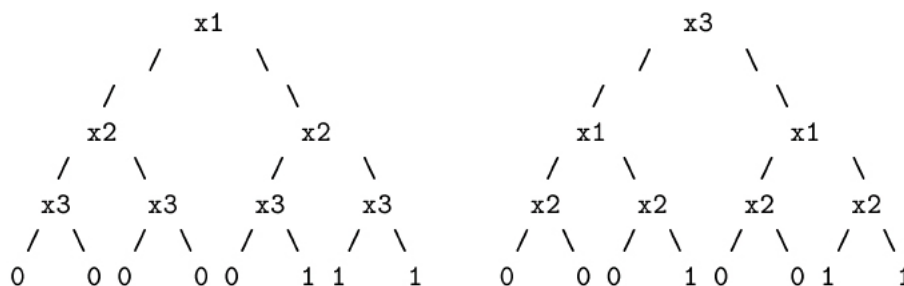


Figure 1: S-trees for the function x_1 and $(x_2 \text{ or } x_3)$

In the picture, the two S-trees represent the same Boolean function:

$$f(x_1, x_2, x_3) = x_1 \text{ and } (x_2 \text{ or } x_3)$$

For the left tree, the variable ordering is x_1, x_2, x_3 , and for the right tree it is x_3, x_1, x_2 . The values of the variables x_1, \dots, x_n , are given as a Variable Value Assignment (VVA) ($x_1 = b_1, x_2 = b_2, \dots, x_n = b_n$) with $b_1, b_2, \dots, b_n \in \{0, 1\}$. For instance, $(x_1 = 1, x_2 = 1, x_3 = 0)$ would be a VVA for $n = 3$, resulting, for the sample function above, in the value $f(1, 1, 0) = 1$ and $(1 \text{ or } 0) = 1$.

Your task is to write a program which takes an S-tree and some VVAs and computes $f(x_1, \dots, x_n)$ as described above.

1.1 Input Format

The input contains the description of several S-trees with associated VVAs which you have to process. Each description begins with a line containing a single integer n , $1 \leq n \leq 7$, the depth of the S-tree. This is followed by a line describing the variable ordering of the S-tree. The format of

that line is $x_{i_1}x_{i_2}\dots x_{i_n}$. (There will be exactly n different single space-separated strings). So, for $n = 3$ and the variable ordering x_3, x_1, x_2 , this line would look as follows

x3 x1 x2

In the next line the distribution of 0's and 1's over the terminal nodes is given. There will be exactly 2^n characters (each of which can be 0 or 1), followed by the new-line character. The characters are given in the order in which they appear in the S-tree, the first character corresponds to the leftmost terminal node of the S-tree, the last one to its rightmost terminal node.

The next line contains a single integer m , the number of VVAs, followed by m lines describing them. Each of the m lines contains exactly n characters (each of which can be 0 or 1), followed by a new-line character. Regardless of the variable ordering of the S-tree, the first character always describes the value of x_1 , the second character describes the value of x_2 , and so on. So, the line

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corresponds to the VVA ($x_1 = 1, x_2 = 1, x_3 = 0$).

The input is terminated by a test case starting with $n = 0$. This test case should not be processed.

1.2 Output Format

For each S-tree, output the line "S-Tree # j ", where j is the number of the S-tree. Then print a line that contains the value of $f(x_1, x_2, \dots, x_n)$ for each of the given m VVAs, where f is the function defined by the S-tree. Output a blank line after each test case.

1.3 Sample Input

```
1 3
2 x1 x2 x3
3 00000111
4 4
5 000
6 010
7 111
8 110
9 3
10 x3 x1 x2
11 00010011
12 4
13 000
14 010
15 111
16 110
17 0
```

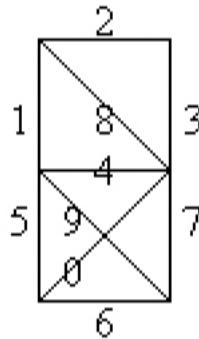
1.4 Output for the Sample Input

```
1 S-Tree #1  
2 0011  
3  
4 S-Tree #2  
5 0011  
6
```

2 Led Codes

Source file name: `ledcode.c`, `ledcode.cpp` or `ledcode.java`

Some led systems display characters as a combination of lightlines, much like digital calculators do. Suppose we have one of such led systems, in which each letter of the standard English alphabet is constructed combining some of ten possible lightlines, numbered as below:



For instance, the letter A is shown using the lines 1, 2, 3, 4, 5 and 7. With these few lines it is not possible, of course, to show all the 26 letters with their natural shapes. A complete list of the letters of our system is appended at the end.

You have to solve the problem of decoding a combination of numbers (representing lightlines) in the form of the respective letter, to form a whole word or phrase. As input you have a string of letters and/or numbers, and as output you must show only the letters.

2.1 Input Format

The input begins with a line containing a single integer N , that indicates the number of input examples, followed by N lines, each one representing an input phrase. Each input phrase consists of lowercase letters, blank spaces and/or digits. In the case of digits, their combination must form valid led letters. Each letter is coded as a combination of numbers, ordered in the form 1, 2, 3, 4, 5, 6, 7, 8, 9, 0. A zero (0) that is not part of a valid letter code, is interpreted as a blank space.

You may assume that no invalid codes are entered, and that the system does not allow ambiguity between two letter codes.

2.2 Output Format

The output consists of N lines (one for each input string) with the form:

Phrase 1:

Phrase 2:

where the dots are, of course, the result of the decoding process. The alphabetic letters and blank spaces must not be decoded at all: only the numbers must be converted to the corresponding led letters.

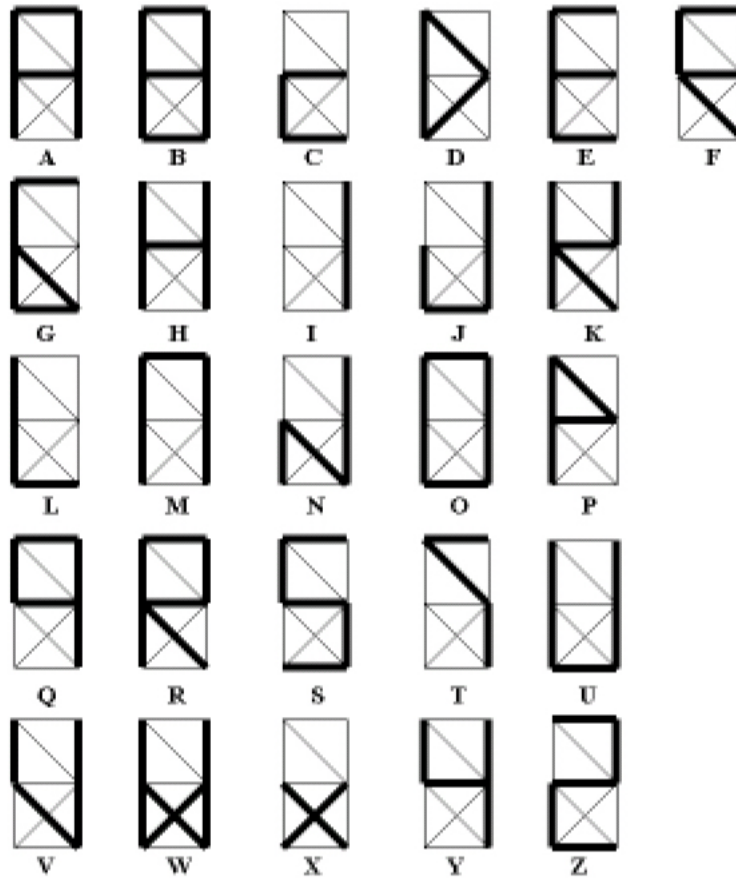
2.3 Sample Input

```
1 3
2 HELL1235670W01234591561580
3 PROGRAMMING037124670C123567123567156
4 AND MORE037124903735790278134573712467045612356735792781245612467278
```

2.4 Output for the Sample Input

```
1 Phrase 1: HELLO WORLD
2 Phrase 2: PROGRAMMING IS COOL
3 Phrase 3: AND MORE IF IN THIS CONTEST
```

2.5 Complete List of Letters



3 Cable Network

Source file name: cn.c, cn.cpp or cn.java

A local cable network is planning to expand their services to a neighboring city. For that, a transmission center is being built and a cable net connecting the new clients has to be installed. Each client has to be connected to the center in the cable net.

The network organized a survey and has now the addresses of all potential clients. Also it has an estimate on the cost of installing each cable link through the city.

The network board of directors has decided to offer the following initial subscription package: Each new client will pay a fixed subscription fee and will get the first three months of service for free. This ensures a **potential initial capital** for building the cable net, which is simply the number of potential clients (according to the survey) multiplied by the subscription fee.

The decision on what links to build in this first phase will be done according to the following. A set of links induces a **loss in the potential initial capital**, defined as $l + (t \times d)$, where l is the cost of installing the links in the set, t is the subscription fee and d is the number of potential clients that are **not** connected to the center by this set of links. The board of directors decided they will build a set of links that induces a loss as small as possible in the potential initial capital.

Your job is to write a program to compute the minimum possible loss in the potential initial capital. For that, you are given the location of each potential client as well as the center location. Also, you are given the costs of all possible net links and the value of the subscription fee.

3.1 Input Format

The input contains the description of several instances. An instance with $n = 0$ indicates the end of the input. Your program should not process this instance.

The first line contains two positive integers: n ($0 \leq n \leq 20$) representing the number of potential clients and t representing the subscription fee. Each potential client is identified by a number between 1 and n while the center is identified by 0. Next, there is a line for each i from 0 to $n - 1$. In line i there is a list of $n - i$ positive integers. Each integer, say the j -th one, represents the cost of installing a link between i and j .

3.2 Output Format

For each instance, your program should print three lines; the first contains "Cable Net # j ", where j is the number of the instance; in the second line, it should print the potential initial capital for that instance and in the third line, the value of the minimum possible loss in the potential initial capital for that instance. Your program should also print a blank line after the output of each instance.

3.3 Sample Input

```
1 5 10
2 5 17 2 3 23
3 9 6 1 19
4 14 5 13
5 19 21
6 40
7 3 1
8 5 3 23
9 1 19
10 14
11 0 1
```

3.4 Output for the Sample Input

```
1 Cable Net #1
2 50
3 21
4
5 Cable Net #2
6 3
7 3
8
```

4 Bomb the Bridge

Source file name: bridge.c, bridge.cpp or bridge.java

The Air Force has a special team devoted to destroying bridges. This team is composed of several planes which fly over the targeted bridge one after another. Each of these planes carries one bomb, which the pilot drops at a given location in the bridge. The aim of the team is to split the bridge in two, so that no one can cross it.

Unfortunately, bombs are not completely accurate. As a result, even though missions are planned in advance, the exact location where the bombs actually fall may be different than planned. Still, the Air Force keeps his original plan untouched except for the last plane, which may have to act differently.

Each bomb that is dropped on the bridge leaves a hole that, viewed from above, has the shape of a circle, its radius depending on the power of the bomb. A bomb of size s leaves a hole of radius s . Your task is to determine the plan for the last plane, that is, the minimum bomb size and the position where the last plane should drop the bomb so that, if everything goes well, the bridge is split in two.

4.1 Input Format

The first line contains a positive integer n , representing the number of instances of the problem contained on the input.

Each instance is represented by three positive integers w , ℓ and b , which denote the width and length of the bridge and the amount of bombs dropped on the bridge. Then come b lines, each containing integers x , y and r ($x, y \geq 0$, $r > 0$) which denote the coordinates of the center and the radius of the holes left by the b bombs. Coordinate $(0,0)$ is the lower-left corner of the bridge (viewed from above), assuming that the bridge has width parallel to the x axis and length parallel to the y axis.

4.2 Output Format

Your program must produce one output line for each instance. This line contains an **integer** representing the minimum bomb size you need to split the bridge in two, or the words **Bridge already split** if the bridge is already split by the bombs that have been dropped. The bridge is considered to be split if the two ends of the bridge are disconnected (except perhaps for a finite number of points). Remember that a bomb of size s leaves a hole of radius s .

4.3 Sample Input

```
1 3
2 100 1000 2
3 15 100 20
4 90 100 30
5 100 1000 1
6 50 100 40
7 100 1000 2
8 25 500 25
9 75 500 25
```

4.4 Output for the Sample Input

```
1 13  
2 50  
3 Bridge already split
```

5 Move the Water

Source file name: `water.c`, `water.cpp` or `water.java`

You have three jars containing water. Each jar has associated a capacity indicating the maximum amount of water it can contain. Your wish is to have a certain amount of water in each jar. The initial content of each jar, its capacity, and the desired content, are all non negative integers; in addition, the capacities are between 1 and 150. You have nothing but the jars to help you in achieving your goal. So the only way to obtain the desired content in each jar is to make a sequence of *movements* of water. In a movement of water you pour a certain amount of water from one jar to another jar. We call the first jar *source* and the second jar *destination*. While moving water two situations can occur: If the current content of the source jar is not enough to complete the capacity of the destination jar, then all the water contained in the source jar is moved to the destination jar; otherwise, only the exact amount of water needed to complete the destination jar is moved from the source jar. Under no circumstances you can use additional water or throw away water. Your task is to determine the minimum number of movements required to obtain the desired amount of water in each jar.

Input Format

The input contains a certain number of test cases for this problem. Each test case is given in a single line containing nine values $c_1, c_2, c_3, a_1, a_2, a_3, b_1, b_2, b_3$; these values are separated by an arbitrary number of blank spaces. The value c_i is the capacity of the i -th jar, a_i is its initial content, and b_i is the desired content for the jar. In the last line of the input c_1 has value equal to 0; this line should not be processed.

Output Format

For each test case in the input, the output must contain a line with the minimum number of movements required to obtain the desired content in each jar. If for a given test case there is no solution, you must write the value -1 instead of the number of movements.

Sample Input

```
1 5 4 1 1 0 1 0 2 0
2 5 4 1 1 0 1 0 3 0
3 5 4 1 1 0 1 0 0 2
4 5 4 1 1 0 1 1 0 1
5 5 4 1 0 4 0 3 0 1
6 0 1 1 0 0 0 0 0 0
```

Output for the Sample Input

```
1 2
2 -1
3 -1
4 0
5 2
```

6 Faking Mondrian

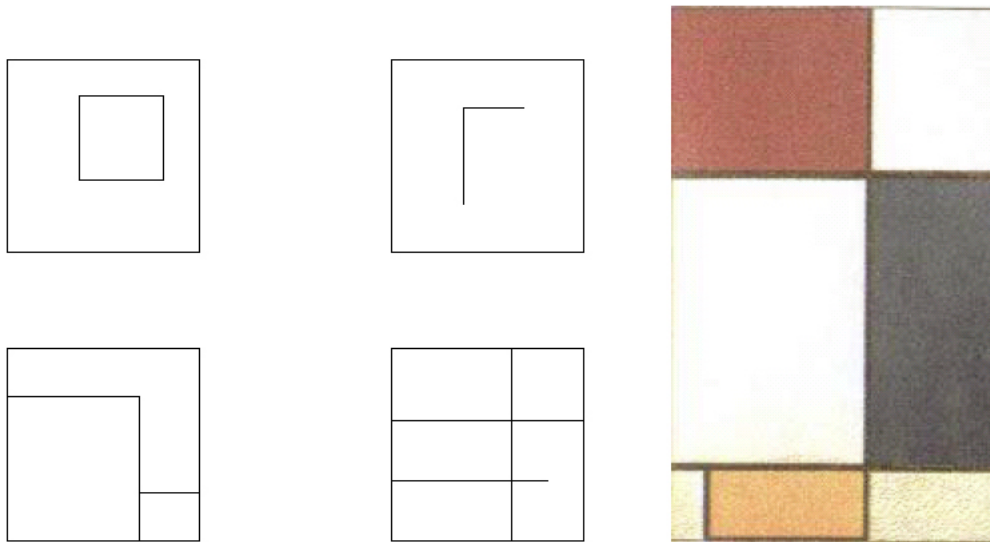
Source file name: `mondrian.c`, `mondrian.cpp` or `mondrian.java`

Piet Mondrian (1872-1944) was one of the best abstract artists of the century. His simple yet elegant designs were intentionally restricted to use only straight lines and a few colors. His artwork reflects an idealized view of reality, one which has perfect harmony and balance.

Armando, a Latin American businessman, wants to create and sell fake Mondrian pictures. Since Mondrian's designs are based on a few simple rules, he hopes to build a machine that can mass-produce different Mondrian pictures and sell them as originals.

Mondrian's rules are very simple:

1. only black, white, red, blue and yellow colors can be used.
2. the painting can only contain rectangles, with sides parallel to the borders of the canvas. Lines that are not part of the border of a rectangle are not allowed. The following four examples do not fulfill this rule:



The top-left painting contains a shape that is not a rectangle (the shape that is outside the central square). In the top-right painting every shape is a rectangle, but there are lines that are not part of the border of any rectangle. Bottom-left painting contains a shape that is not a rectangle (the inverted L). Bottom-right painting contains a line that is not part of the border of any rectangle. In the figure we also include a real (well, sort of) Mondrian (Composition with red, yellow, and blue, 1928).

3. Borders of the rectangles can only be painted in black. Rectangles can only be painted in white, red, blue or yellow. The borders of the canvas are considered to be already painted in black.
4. Two adjacent rectangles (that is, two rectangles that share a segment of their borders) cannot have the same color, unless they are painted in white.

The machine Armando has devised receives a set of instructions to draw the painting. Your task is to program an algorithm that will tell (before the machine begins to perform Armando's instructions)

whether these instructions correspond to a picture that fulfills Mondrian's rules, and how much paint he will need.

6.1 Input Format

The input contains a set of test cases. Each test case is described in several lines, and contains Armando's instructions for one painting. There are two types of instructions: instructions that indicate the drawing of a line, and instructions that indicate the painting of a rectangle. Each test case of the input starts with a line containing four integer values w, h, n, m . The values w and h represent the width and height of the canvas, respectively; these values are between 1 and 10000. The value n is the number of instructions for drawing lines, while m is the number of instructions for painting rectangles; these values are between 0 and 1000. The test case continues with n lines containing the instructions for drawing lines, each instruction in a separate line. Each instruction consists of four integer values x_1, x_2, x_3 and x_4 , where (x_1, x_2) and (x_3, x_4) are the coordinates of the end points of the line. Lines are always horizontal or vertical. The lower left corner of the canvas has coordinates $(0, 0)$. Instructions can result in a line or part of a line being drawn more than once. The test case ends with m lines containing the instructions for painting rectangles, each one in a separate line of the input. Each instruction specifies two integer values x and y , as well as a letter c in the set $\{r, b, y\}$ (r means red, b is blue and y is yellow). The instruction indicates the machine to paint the rectangle containing the point with coordinates (x, y) with color c . All rectangles not painted with a color in this set are assumed to be painted in white. The input ends with a test case in which w has a value of 0; this test case should not be processed. Every pair of consecutive values in a same line of the input is separated by an arbitrary number of blank spaces.

6.2 Output Format

Your program must produce one output line for each test case. If the instructions follow Mondrian's rules, you must write the line **Mondrian r b y**, where r , b and y are total areas painted in red, blue and yellow, respectively. Otherwise, you must write the line **Error!**.

6.3 Sample Input

```
1 100 100 3 3
2 0 50 60 50
3 20 50 100 50
4 50 0 50 100
5 25 25 r
6 75 75 r
7 25 75 y
8 610 987 2 3
9 0 50 305 50
10 305 0 305 987
11 1 1 r
12 1 400 r
13 400 100 y
14 1000 1000 3 2
15 0 200 500 200
16 500 0 500 400
17 500 400 1000 400
18 200 800 r
19 700 200 y
20 0 0 0 0
```

6.4 Output for the Sample Input

```
1 Mondrian 5000 0 2500
2 Error!
3 Error!
```

7 Editing Distance

Source file name: `dna.c`, `dna.cpp` or `dna.java`

Since the acceptance of Darwin's theory on evolution, many researchers have tried to understand the evolutionary history of living organisms. This study is done normally through the construction of *phylogenetic trees*. Up to 1950, the construction of these trees was based on experiments and intuition. Gradually, mathematical formalism appeared and now, with the development of molecular biology, data about the molecular structure of organisms is being used in these constructions.

One of the sources of data is the evolutionary distance between species. A tentative way to determine this distance is to study the differences between the DNA of two species. A DNA molecule consists of a double chain of basis. There are four basis, each one denoted usually by one of the letters *A*, *C*, *G* or *T*.

The simplest events that occur during the course of molecular evolution are substitution of one base for another and the insertion or deletion of a base-pair. The *editing distance* between the DNA molecules of the two species is the minimum number of these events – deletion, insertion and substitution – that transform a DNA molecule into the other one.

Your mission is to write a program that reads a sequence of pairs of DNA molecules (given by the sequence of basis of one of the chains) and computes, for each pair, its editing distance.

7.1 Input Format

The first line of the input contains a number n ($0 < n \leq 20$), which indicates the number of given pairs of DNA sequences. In each of the next $2n$ lines, there is a sequence of basis, that is, a sequence of *A*, *C*, *G* or *T*, of length at most 200.

7.2 Output Format

The output should consist of n lines, one for each pair of DNA sequences. Each line consists of `Pair #i: editing distance d`, where $i \in \{1, \dots, n\}$ and d is the editing distance of the i th pair of DNA sequences.

7.3 Sample Input

```
1 3
2 ATAAGC
3 AAAAAACG
4 AATCGTATGGCCCTA
5 ATGGTGATGGCCAT
6 GCTCTGCGAATA
7 CGTTGAGATACT
```

7.4 Output for the Sample Input

```
1 Pair #1: editing distance 3
2 Pair #2: editing distance 5
3 Pair #3: editing distance 7
```